THE O.P. GUPTA

ADVANCED MATH CLASSES

Mathematics (Standard & Basic)

Topic - Polynomials



Max. Marks - 40 Time - 90 Minutes

SECTION A

Following multiple choice questions are of 1 Mark each (Q01-10). Select the correct option in each one of them.

Q01. It is given that α and β are the zeroes of the quadratic polynomial $p(x) = x^2 - p(x+1) - c$, such that $(\alpha+1)(\beta+1)=0$, then the value of c is

(A) 0

(C) -1

What should be added to the polynomial $f(x) = x^2 - 5x + 4$, so that 3 becomes a zero of the resulting Q02. polynomial?

(A) 1

(B) -2

(C) 4

The graph of a polynomial p(x) passes through the points (-5, 0), (0, -40), (8, 0) and (5, -30), Q03. then which of the following is a factor of p(x)?

(A) $x^2 - 3x - 40$

(B) $x^2 - 13x - 40$

(C) $x^2 - 25$

(D) None of these

The number of real zeroes of the polynomial $293 x^3 - 293$ is O04.

(A) 0

(B) 1

(C) 2

Q05. If α and β are the zeroes of the polynomial $p(s) = s^2 - a s - b$, then the value of $(\alpha^2 + \beta^2)$ is

(A) $b^2 - 2a$

(B) $b^2 + 2a$

(C) $a^2 + ab$

(D) $a^2 + 2b$

If one zero of the quadratic polynomial $ax^2 + bx + c$ is double the other, then which of the following is O06.

(A) $2b^2 = 9ac$

(B) $3b^2 = 2bc$ (C) $b^2 = 4ac$

(D) $2c^2 = 9ab$

Q07. The quadratic polynomial whose zeroes are $\frac{3+\sqrt{5}}{5}$ and $\frac{3-\sqrt{5}}{5}$, is

(A) $25x^2 - 30x + 4$ (B) $5x^2 - 6x + 4$ (C) $25x^2 - 30x + 20$ (D) $\frac{1}{5}(5x^2 + 6x + 4)$ If 2 and $\frac{1}{2}$ are the zeroes of $px^2 + 5x + r$, then

(A) p = r = 2

(C) p = 2, r = -2

(D) p = -2, r = 2

Followings are Assertion-Reason based questions (Q09 & 10).

In the following questions, a statement of Assertion (A) is followed by a statement of Reason (R). Choose the correct answer out of the following choices.

- (A) Both **A** and **R** are true and **R** is the correct explanation of **A**.
- (B) Both **A** and **R** are true and **R** is not the correct explanation of **A**.
- (C) A is true but R is false.
- (D) A is false but R is true.
- Assertion (A): If a quadratic polynomial has equal zeroes, then its graph touches the x-axis at exactly Q09. one point.

Reason (R): A quadratic polynomial represented by $ax^2 + bx + c$, $a \ne 0$ has equal zeroes, if and only if its discriminant $(b^2 - 4ac)$ is a non-negative and non-zero real number.

Assertion (A): The graph of the quadratic polynomial $ax^2 + bx + c$ opens upwards, if a > 0. Q10. Reason (R): The sign of the coefficient 'a' in the quadratic polynomial determines the direction in which the parabola opens.

 $[1 \times 10 = 10]$

SECTION B

Followings are of 2 Marks each (Q11-12).

Find the zeroes of the polynomial $t^2 - 3t - m(m+3)$.

Q12. (a) If $(x-\alpha)$ is a factor of two quadratic polynomials $x^2 + px + q$ and $x^2 + mx + n$, then prove that $\alpha = \frac{n-q}{p-m}$.

OR

(b) If sum of the zeroes of $5x^2 + (p+q+r)x + pqr$ is zero (0), then find the value of $p^3 + q^3 + r^3$.

$$[2 \times 2 = 4]$$

SECTION C

Followings are of 3 Marks each (Q13-16).

- Q13. If α and β are the zeroes of the polynomial $f(t)=t^2-3t-2$, then find a quadratic polynomial whose zeroes are $\left(\frac{1}{2\alpha+\beta}\right)$ and $\left(\frac{1}{2\beta+\alpha}\right)$.
- Q14. If α and β are the zeroes of $f(y) = 2y^2 + 5y + k$ and they satisfy the relation $\alpha^2 + \beta^2 + \alpha\beta = \frac{21}{4}$, then find the value of k.
- Q15. (a) If the squared difference of the zeroes of $g(t) = t^2 + pt + 45$ is 144, then find the value (s) of p.

OR

- (b) If α and β are the zeroes of polynomial $25x^2 15x + 12$, then find a quadratic polynomial whose zeroes are $\frac{1}{2\alpha}$ and $\frac{1}{2\beta}$.
- Q16. If α and β are the zeroes of the polynomial $x^2 6x + a$, find the value of a, if $3\alpha + 2\beta = 20$.

 $[3 \times 4 = 12]$

SECTION D

Followings are of 5 Marks each (Q17-18).

- Q17. If α and β are the zeroes of the polynomial $f(x) = x^2 px + q$, prove that $\frac{\alpha^2}{\beta^2} + \frac{\beta^2}{\alpha^2} = \frac{p^4}{\alpha^2} \frac{4p^2}{\alpha} + 2$.
- Q18. (a) If α and β are the zeroes of the quadratic polynomial $f(x) = ax^2 + bx + c$, then find the value of $a\left(\frac{\alpha^2}{\beta} + \frac{\beta^2}{\alpha}\right) + b\left(\frac{\alpha}{\beta} + \frac{\beta}{\alpha}\right)$.

OR

(b) If α and β are the zeroes of quadratic polynomial $p(x) = 6x^2 + x - 1$, then determine the value of $\frac{\alpha}{\beta} + \frac{\beta}{\alpha} + 2\left(\frac{1}{\alpha} + \frac{1}{\beta}\right) + 3\alpha\beta$.

 $5 \times 2 = 10$

SECTION E

Following is a case-study based question of 4 Marks (Q19); having three sub-parts (i), (ii) and (iii).

Q19. A drone is sent on a surveillance mission along a straight road.



The diagram shown is for the representation purpose only.

The drone's height h(t) in metres at time t seconds is given by the polynomial

$$h(t) = -5t^2 + 40t + 100,$$

which represents the drone's height from the moment it starts vertically up from the base station at t = 0, till it comes back down.

Based on the above information, answer the questions given below.

- (i) Find the initial height of the drone.
- (ii) At what time will the drone reach its maximum height?
- (iii) (a) Factorize the polynomial $h(t) = -5t^2 + 40t + 100$ and hence find the time when the drone is at ground level.

OR

(b) Find the zeroes of the polynomial $h(t) = -5t^2 + 40t + 100$ and verify the relationship between the zeroes obtained and coefficients of the polynomial h(t).

$$[1+1+2=4]$$

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